$\mathcal{AMoR}_{\mathcal{E}}$ a package for $\mathcal{A} ext{-utomatic }\mathcal{Mo} ext{-lecular }\mathcal{R}_{\mathcal{E}} ext{-placement}$

Writeup

Jorge Navaza¹ C.N.R.S. France

 $^{^1}Acta$ Crystallographica A50, 157-163. (1994) " \mathcal{AMoRe} : an Automated Package for Molecular Replacement".

JOB

JOB creates default inputs and a script with a tentative protocol to solve the molecular replacement problem.

Calling command: ./e/job dato

```
Input:
         ./i/dato.i3 = input described below.
         ./d/data.d = main \mathcal{AMORE} input described below.
Output:
         ./job
                       = script with protocol for the actual molecular
                          replacement problem.
         ./i/sort.i1
                       = input for SORTING.
         ./i/patt.i1
                       = input for PATTING.
         ./i/tabl.i1
                         input for TABLING.
         ./i/oicrd.i2
                      = input for OIC (ROTING mode).
         ./i/oicto.i2
                       = input for OIC (TRAING mode, one-body).
         ./i/oictn.i2
                         input for OIC (TRAING mode, n-body).
                       = input for OIC (FITING mode).
         ./i/oicfd.i2
         ./i/oicpr.i2
                      = input for OIC (PROPRE mode).
```

Input: file ./d/data.d

```
* D44HEL **
99.7 167.3 84.7 90. 90. 90.
x,y,z * 1/2+x,1/2-y,-z * 1/2-x,-y,1/2+z * -x,1/2+y,1/2-z * end
0
95. 0.
15. 3.5
2 2 2
```

Description

- 1) Title (format A80).
- 2) Cell.
- 3) Symmetry operations (lower case), finishing '* end'.
- 4) NORT Code to define an orthogonal reference frame.
- 5) PERC BADD

```
PERC = uses only the PERC % highest F<sup>obs</sup>.

BADD = B-factor added to F<sup>obs</sup> (e.g. -5 to sharpen data).
```

6) DMAX DMIN

Resolution limits used for the molecular replacement problem (in Å).

7) NTYP MOL1 ... MOLn

```
\begin{array}{lll} {\rm NTYP} & = & {\rm number\ of\ different\ models}. \\ {\rm MOL}\{\#\} & = & {\rm number\ of\ molecules\ of\ model-type\ }\{\#\}\ {\rm in\ the\ a.u.}; \\ & & \{\#\} = 1, {\rm NTYP}. \end{array}
```

Input: file ./i/dato.i3

```
job +*+*+*+*+*+*+*+*
xyz
1. 2 10 0.5 2.5
c-o 50 0.3 30
p-t 10 0.5 30
10 20
20.
```

- Keyword (format A4) = 'job'.
- 2) AKEY (format A5)

Keyword defining mode: 'xyz' reads coordinates; 'map' reads electron density map.

RATE LMINS LMINF CUTR STEP 3)

> RATE defines the integration radius as RATE × Molrad, where Molrad = radius of the smallest sphere, with origin at CoM, containing the whole molecule.

several rotation functions are calculated, where the spherical-LMINs harmonics expansions begin with LMINs $< \ell <$ LMINf; the LMINf ℓ -expansion controls the angular resolution.

= cutoff in rotation function output; first selects all peaks CUTR above CUTR × maximum-peak-height.

step size for ϕ , θ and ψ (in degrees). STEP

TKEY NUMR CUTT NPIC (format A5,*)

computes centered-overlap;

'p-t' computes phased-translation ('p-t-f' when phases are available);
'h-l' computes Harada-Lifchitz translation function; TKEY

computes correlation-coefficient.

selects up to a maximum of NUMR orientations for input NUMR to one-body translations.

CUTT = cutoff in fast translation function output; first selects all peaks above CUTT × maximum-peak-height of 'c-o', 'p-t', 'h-l' or 'c-c' fast translation function.

NPIC number of peaks to output of translation function. The program computes correlations and R-factors.

- Same as previous card, but for n-body translations (it must be present, even if not used).
- NUMT NITE

selects up to a maximum of NUMT positions to refine. NUMT

number of iterations in the least-squares procedure. NITE

7) CUTD

Cutoff to eliminate positions with CoM-CoM distance less than CUTD A.

Example

The data.d file corresponds to a crystal with two molecules of the complex Fab-Lysozyme in the asymmetric unit, and two search models (Fab = 1, Lysozyme = 2). JOB proposes the following protocol:

```
# amore
./e/sorting
  set k=1
  while (\$\{k\} \le 2)
./e/tabling ${k}
  set k=\text{`expr } \{k\} + 1
  end
  set k=1
  while (\{k\} <= 2)
./e/oic\_roting oicrd \{k\} o\{k\}r
  set k=\text{`expr } \{k\} + 1
  end
cat ./o/o*r.s > ./o/or1.s
./e/oic_traing oicto or1 ot1
  set k=1
  while (\$\{k\} < 4)
  set m=\text{`expr } \{k\} + 1
./e/oic\_traing oictn ot \{k\} ot \{m\}
  set k=\text{`expr } \{k\} + 1
  end
./e/oic_fiting oicfd ot4 of4
./e/mr2ic of4 mr2ic
```

Note that all the one-body rotation outputs (./o/o{#}r.s) have been concatenated into the single file ./o/or1.s. However, since we may expect the Fab positions to be determined more easily than the Lysozymes, we may execute the programs in a different order:

```
# amore
./e/sorting
  set k=1
  while (\$\{k\} \le 2)
./e/tabling ${k}
  set k = 'expr \$\{k\} + 1'
  end
  set k=1
  while (\$\{k\} \le 2)
./e/oic\_roting oicrd $\{k\} o$\{k\}r
  set k='expr $\{k\} + 1'
  \quad \text{end} \quad
./e/oic_traing oicto o1r ot1
./e/oic_traing oictn ot1 ot2
./e/oic_fiting oicfd ot2 of2
./e/oic_traing oictn o2r of2 ot3
./e/oic_traing oictn ot3 ot4
./e/oic_fiting oicfd ot4 of4
./e/mr2ic of 4 mr2ic
```

Note that fast rigid-body refinement is performed on the 2-body translation output.

SORTING

SORTING packs and sorts $H,K,L,F^{\mbox{obs}}$ for use in later programs. The packing is cell and space-group dependent.

Calling command: ./e/sorting

Input: file ./i/sort.i1

```
sorting +*+*+*+*+*+*+*+*+*
1 10 9 :logical units
* D44HEL **
99.7 167.3 84.7 90. 90. 90.
x,y,z * 1/2+x,1/2-y,-z * 1/2-x,-y,1/2+z * -x,1/2+y,1/2-z * end 15.00 3.50
1.00
```

- 1) Keyword (format A7) = 'sorting'.
- 2) LUN1 LUN2 LUN3

Logical units (see script ./e/sorting):

 $LUN1 = input ascii file of H,K,L,F^{obs} (./d/hkl.d).$

LUN2 = output binary file of packed and sorted H,K,L,F^{obs}

(./f/xudi).

LUN3 = SORTING output (./o/sort.s).

- 3) Title (format A80).
- 4) Cell.
- 5) Symmetry operations (lower case), finishing '* end'.
- 6) DMAX DMIN

Resolution limits. Performs statistics for data within this resolution range.

7) SCAL

Dividing scale factor.

PATTING

PATTING calculates the Patterson function using the expression

$$P(\mathbf{r}) = \frac{1}{V} \sum_{\mathbf{H}} |F_{\mathbf{H}}|^2 e^{-2\pi i \mathbf{H} \mathbf{r}}$$

Calling command: ./e/patting

Input: ./i/patt.i1 = input described below.

 $./f/xudi = binary file of packed and sorted H,K,L,F^{obs}.$

Output: ./o/patt.s = PATTING output.

To recover the Patterson function map, erase in script ./e/patting the symbol "#" in line "#mv \$AMOREF/fort.91 patmap". ./patmap is a binary file with several registers:

```
real patmap(nx,ny,nz)
write(file) nx,ny,nz,a,b,c,alpha,beta,gamma
do iz=1,nz
write(file) ((patmap(ix,iy,iz),ix=1,nx),iy=1,ny)
enddo
```

where:

nx,ny,nz = number of sampling points in each direction. a,b,c,alpha,beta,gamma = cell parameters (in Å and degrees).

Input: file ./i/patt.i1

```
patting +*+*+*+*+*+*+*+*+*
2 1 1 :printing
10 9 :logical units
* D44HEL **
99.7 167.3 84.7 90. 90. 90.
x,y,z * 1/2+x,1/2-y,-z * 1/2-x,-y,1/2+z * -x,1/2+y,1/2-z * end
90. 0.
15.00 3.50 1.00
0.10 100 1.e-4
```

- 1) Keyword (format A7) = 'patting'.
- 2) Printing options.
- 3) LUN1 LUN2

Logical units (see script ./e/patting):

LUN1 = input binary file of packed and sorted H,K,L,F^{obs} (./f/xudi).

LUN2 = PATTING output (./o/patt.s).

- 4) Title (format A80).
- 5) Cell.
- 6) Symmetry operations (lower case), finishing '* end'.
- 7) PERC BADD

PERC = uses only the PERC % highest F^{obs}.

BADD = B-factor added to F^{obs} (e.g. -5 to sharpen data).

8) DMAX DMIN SHAR

DMAX,DMIN = data resolution limits.

SHAR = Shannon rate (the greater SHAR, the finer the mesh).

Defines the crystal cell sampling as

 $NX \approx 2 \times a / (DMIN/SHAR)$

 $NY \approx 2 \times b / (DMIN/SHAR)$

 $NZ \approx 2 \times c / (DMIN/SHAR)$

9) CUTP NPIC DELT

CUTP = cutoff in Patterson function; selects all peaks above

 $CUTP \times maximum-peak-height.$

NPIC = maximum number of peaks to output of Patterson function.

DELT = used in peak-search to avoid spurious peaks.

TABLING

TABLING calculates the array of molecular scattering factors corresponding to the model coordinates. Puts the model in a small model-box: first translates the coordinates so that the center of mass is at the origin, and rotates the coordinates so that the model's principal axes of inertia are parallel to the model-box axes. The model-box is put in a big cell in order to sample the model Fourier transform finely, to allow structure factors and gradients of the rotating model to be accurately interpolated.

For given orientation ${\bf R}$ and translation ${\bf T}$ of the search model, the calculated structure factors are expressed in terms of the model scattering factors – f_m – by

$$F_{\mathbf{H}}^{cal\,(m)}(\mathbf{R}, \mathbf{T}) = \sum_{g=1}^{G} f_m(\mathbf{H}\mathbf{M}_g \mathbf{D}\mathbf{R}\mathbf{O}_m) e^{2\pi i \mathbf{H} \left(\mathbf{M}_g \mathbf{T} + \mathbf{t}_g\right)}$$

Calling command: ./e/tabling {#}

Input: ./i/tabl.i1 = input described below.

\$AMORE/factor.d = ascii file of atomic form-factors.

./d/xyz{#}.d = ascii file of coordinates.

./d/map{#}.d = binary file of electron density.

Output: ./f/tabl{#} = binary file of molecular scattering factors.

./o/tabl{#}.s = TABLING output.

Input: file ./i/tabl.i1

- 1) Keyword (format A7) = 'tabling'.
- 2) Printing options.
- 3) LUN1 LUN2 LUN3 LUN4

Logical units (see script ./e/tabling):

 $LUN1 = input ascii file of coordinates - ./d/xyz{#}.d$

 $LUN2 = input binary file of electron density - ./d/map{#}.d$

LUN3 = output binary file of molecular scattering factors $-./f/tabl\{\#\}$

 $LUN4 = TABLING output - ./o/tabl{#}.s$

4) Title (format A80).

The procedure uses "sed" to add "model $\{\#\}$ -" to the title.

5) AKEY (format A5)

Keyword defining mode: 'xyz' reads coordinates; reads electron density map.

6) BFLG BREP

B-factor flags:

BFLG = 1, replace all atomic B-factors by BREP.

BREP = to set all atomic B-factors to BREP.

7) SBOX

Defines the model-cell as SBOX \times model-box.

8) DMIN SHAR TFLG BADD

DMIN = resolution limit of generated Fourier coefficients. In

fact program generates past this point to allow for

interpolation at the frontier.

SHAR = Shannon rate (the greater SHAR, the finer the mesh).

Defines the model-cell sampling as

 $NX \approx 2 \times \tilde{a} / (DMIN/SHAR)$

 $NY \approx 2 \times \tilde{b} / (DMIN/SHAR)$

 $NZ \approx 2 \times \tilde{c} / (DMIN/SHAR)$

where $\tilde{a}, \tilde{b}, \tilde{c}$ are the model-cell parameters.

TFLG = 0, use optimal values for SHAR and BADD.

BADD = "B-factor" to smear the atomic electron density. It is

added in direct space (when reading atomic coordinates)

and subtracted in reciprocal space (in all cases).

Maps

If the search model is an electron density (e.g. a low resolution envelop), TABLING translates it as previously described, but does not rotate it. The input must be a binary file $-./d/map\{\#\}.d$ – with several registers:

```
\begin{array}{l} {\rm real\ rho(mx,my,mz)} \\ {\rm write(file)\ mx,my,mz,xlw,ylw,zlw,xup,yup,zup,alpha,beta,gamma} \\ {\rm do\ iz=}1,{\rm mz} \\ {\rm write(file)\ ((rho(ix,iy,iz),ix=}1,{\rm mx}),iy=}1,{\rm my}) \\ {\rm enddo} \end{array}
```

where:

```
\begin{array}{lll} mx, my, mz & = & number \ of \ sampling \ points \ in \ each \ direction. \\ xlw, ylw, zlw, xup, yup, zup & = & lower \ and \ upper \ limits \ (in \ \mathring{A}) \ of \ the \ model-box. \\ alpha, beta, gamma & = & model-box \ angles. \end{array}
```

The model-box edges are thus

```
\begin{array}{lll} \tilde{a} & = & \text{xup-xlw} \\ \tilde{b} & = & \text{yup-ylw} \\ \tilde{c} & = & \text{zup-zlw} \end{array}
```

This should be, as far as possible, the smallest box containing the model density. The sampling must be sensibly equal to

```
\begin{array}{lll} \text{mx} & \approx & 2 \times \tilde{a} \ / \ (\text{DMIN/SHAR}) \\ \text{my} & \approx & 2 \times \tilde{b} \ / \ (\text{DMIN/SHAR}) \\ \text{mz} & \approx & 2 \times \tilde{c} \ / \ (\text{DMIN/SHAR}) \end{array}
```

Fourier Coefficients

It is also possible to provide the output of TABLING without executing the program. It must be a binary file – ./f/tabl $\{\#\}$ – with two registers:

```
complex fto(-1:hsup,-ksup:ksup,-lsup:lsup)
write(file) a,b,c,alpha,beta,gamma,nort,hsup,ksup,lsup,sqhsup
write(file) fto
```

where:

a,b,c,alpha,beta,gamma = model-cell.

nort = orthogonalising code.

hsup,ksup,lsup = maximum indices of the array; the (h,k,l)

indices run, respectively, within the limits

(-1:hsup), (-ksup:ksup), (-lsup:lsup)

sqhsup = $1/DMIN^2$.

fto = array of complex molecular scattering factors.

In this case, it may be useful to provide also the ./o/tabl{#}.s file, which is used by program OIC to define the integration radius and the model-cell for cross-rotation function calculations.

ROTING

ROTING calculates fast rotation functions (self-, cross- and locked-rotation functions). The rotation function (Patterson Overlap) is defined by

$$PO(\mathbf{R}) = \frac{1}{v} \int_{\mathbf{Q}} P^{(t)}(\mathbf{r}) P^{(s)}(\mathbf{R}^{-1}\mathbf{r}) d^3\mathbf{r}$$

where $P^{(t)}$ and $P^{(s)}$ are the target and search Patterson functions, respectively. Note that the rotation applied to the search model is \mathbf{R} . By expanding the Patterson functions in spherical harmonics, PO may be casted into the form

$$PO(\phi, \theta, \psi) = \sum_{\ell=LMIN}^{LSUP} \sum_{m,m'=-\ell}^{\ell} \left[\sum_{n=1}^{N} \overline{e_{\ell,m,n}^{(t)}} \ e_{\ell,m',n}^{(s)} \right] \ d_{m,m'}^{\ell}(\theta) \ e^{i(m\phi+m'\psi)}$$

with

$$e_{\ell,m,n} = \sqrt{12\pi(2(\ell+2n)-1)} \sum_{\mathbf{H}} \frac{|F_{\mathbf{H}}|^2}{V} Y_{\ell,m}(\mathbf{H}/H) \frac{j_{\ell+2n-1}(2\pi HR)}{2\pi HR}$$

Calling command: ./e/roting {INP} {#} {OUT}

```
Input: ./i/{INP}.i1 = input described below.

./f/xudi = binary file of packed and sorted H,K,L,F<sup>obs</sup>.

./f/tabl{#}.d = binary file of molecular scattering factors for model {#}.

Output: ./f/elmx{#} = binary file of spherical-harmonics expansion coefficients for the crystal.

./f/elmn{#} = binary file of spherical-harmonics expansion coefficients for model {#}.

./o/{OUT}.s = rotation function output.
```

To recover the rotation function map, erase in script ./e/roting , the symbol "#" in the line "#mv \$AMOREF/fort.93 rotmap". ./rotmap is a binary file with several registers:

```
\begin{array}{l} {\rm real\ rotmap(np,nf,nt),theta(nt)} \\ {\rm write(file)\ np,nf,nt,p,f,(theta(n),n=1,nt)} \\ {\rm do\ n=1,nt} \\ {\rm write(file)\ ((rotmap(ip,if,n),ip=1,np),if=1,nf)} \\ {\rm enddo} \end{array}
```

where:

```
\begin{array}{lll} np,nf,nt & = & number\ of\ sampling\ points\ in\ each\ direction.\\ p,f & = & \psi\ and\ \phi\ Euler\ cell\ dimensions\ (in\ degrees).\\ (theta(n),\ n=1,nt) & = & \theta\ sampling\ set\ (in\ degrees). \end{array}
```

Input: file ./i/{INP}.i1 (general form)

Description

- 1) Keyword (format A7) = 'roting'.
- 2) Printing options.
- 3) MKEY (format A4)

Keyword defining mode:

'gene' generates model structure factors in a suitable cell;

'elmn' calculates spherical- harmonics expansion coefficients for crystal or models;

'rota' calculates rotation functions.

The three modes may be used independently.

Different modes:

"gene" mode:

- 1) MKEY (format A4) = 'gene'.
- 2) LUN1 LUN2

Logical units (see script ./e/roting):

LUN1 = input binary file of molecular scattering factors $(./f/tabl\{\#\})$.

LUN2 = output binary file of packed and sorted Fourier coefficients (as produced by SORTING).

- 3) Title (format A80).
- 4) Model cell for rotation function (default cell = model-box + resolution + integration-radius).
- 5) Symmetry operations (lower case), finishing '* end' (usually P1).
- 6) NORT

Code to define an orthogonal reference frame (usually 1).

7) DMAX DMIN

Resolution limits. Generates data within this range (in Å).

8) NBOD

Option to generate structure factors with molecules placed at desired positions (usually 0).

"elmn" mode:

- 1) MKEY (format A4) = 'elmn'.
- 2) LUN1 LUN2

Logical units (see script ./e/roting):

LUN1 = input binary file of packed and sorted Fourier coefficients (as produced by SORTING or ROTING -mode "gene").

LUN2 = output binary file of spherical-harmonics expansion

coefficients (./f/elmx{#} or ./f/elmn{#}).

- 3) Title (format A80).
- 4) Cell.
- 5) Symmetry operations (lower case), finishing '* end'.
- 6) NORT

Code to define an orthogonal reference frame.

7) PERC BADD

 $PERC = uses only the PERC \% highest F^{obs}$.

BADD = B-factor added to F^{obs} (e.g. -5 to sharpen data).

8) DMAX DMIN RMIN RMAX

DMAX

 $\frac{\text{DMIAX}}{\text{DMIN}} = \text{resolution limits.}$

RMIN

 $\frac{RMAX}{RMAX}$ = integration radii (in Å).

"rota" mode:

1) MKEY (format A4) = 'rota'.

2) LUN1 LUN2 LUN3 LUN4 LUN5

Logical units (see script ./e/roting):

LUN1 = input binary file of spherical-harmonics expansion coefficients for fixed crystal (usually ./f/elmx{#}).

LUN2 = input binary file of spherical-harmonics expansion coefficients for rotating crystal (usually ./f/elmn{#}).

LUN3 = rotation function output $(./o/{OUT}.s)$.

LUN4 = input binary file of packed and sorted H,K,L,F^{obs}

(./f/xudi).

LUN5 = input binary file of molecular scattering factors $(./f/tabl\{\#\})$.

- 3) Title (format A80).
- 4) RKEY (format A5)

Keyword defining mode: cross' computes cross-rotation function; self' computes self rotation.

5) LMIN LSUP

Expansions between LMIN and LSUP are used. The ℓ -expansion controls the angular resolution. Low order terms are governed by the crystal symmetry; excluding them may reduce the final peak heights, but make the rotation parameters more precise and make multiple solutions have more equal heights.

6) STEP

Step size for ϕ , θ and ψ (in degrees).

7) NRS1 NRS2

Used to produce several shifts prior to the rotation function calculation (usually 0 0). This allows locked-rotation function calculations.

8) CUTR NPIC DELT

 $CUTR = cutoff in rotation function output; first selects all peaks above <math>CUTR \times maximum-peak-height.$

NPIC = maximum number of peaks to output of rotation function.

DELT = used in peak-search to avoid spurious peaks.

Example

Self Rotation:

The self rotation may be calculated by using the following input cards:

```
roting +*+*+*+*+*+*+*+*
3 0 1 0 :printing
10 91 :logical units
* D44HEL **
99.700 167.300 84.700 90.000 90.000 90.000
x,y,z * 1/2+x,1/2-y,-z * 1/2-x,-y,1/2+z * -x,1/2+y,1/2-z * end
95.0 0.0
15.00 \quad 3.50 \quad 0.00 \quad 42.40
91 0 9 0 0 :logical units
* D44HEL ** self
self
6 500
2.5
0 \quad 0
0.2 1000 0.1E-04
```

If the expansion-coefficients already exist $(./f/elmx\{\#\})$, then the following input may be used:

Locked Cross-Rotation:

The locked cross-rotation is the average of the values of the cross rotation at orientations related by the NCS elements \mathbf{S}_n , n = 1, ..., N:

$$PO_L(\mathbf{R}) = \sum_{n=1}^N PO(\mathbf{S}_n \mathbf{R}) / N$$
.

By redefining the target function, it can be computed as an ordinary cross rotation,

$$PO_L(\mathbf{R}) = \sum_{n=1}^{N} \frac{1}{v} \int_{\Omega} P^{(t)}(\mathbf{r}) P^{(s)}(\mathbf{R}^{-1} \mathbf{S}_n^{-1} \mathbf{r}) d^3 \mathbf{r} / N$$
$$= \frac{1}{v} \int_{\Omega} \left(\sum_{n=1}^{N} P^{(t)}(\mathbf{S}_n \mathbf{r}) / N \right) P^{(s)}(\mathbf{R}^{-1} \mathbf{r}) d^3 \mathbf{r} ,$$

with the target Patterson function substituted by the average over the NCS of the rotated target functions. Let ϕ , θ , ψ be Euler angles of a self-rotation peak; the parameters of the inverse rotation are $\phi' = 180 - \psi$, $\theta' = \theta$, $\psi' = 180 - \phi$. Then, the locked cross-rotation may be calculated by using the following input (N=2):

TRAING

TRAING calculates fast translation functions. The Fourier coefficient of the search model, rotated by **R** and placed at **T**, is given by the expression:

$$F_{\mathbf{H}}^{cal}(\mathbf{T}) = \sum_{g=1}^{G} \left(f_m(\mathbf{H}\mathbf{M}_g \mathbf{D} \mathbf{R} \mathbf{O}_m) e^{2\pi i \mathbf{H} \mathbf{t}_g} \right) e^{2\pi i \mathbf{H} \mathbf{M}_g \mathbf{T}}$$
$$= \sum_{g=1}^{G} u_g^m(\mathbf{H}) e^{2\pi i \mathbf{H} \mathbf{M}_g \mathbf{T}}$$

and the corresponding intensity by

$$I_{\mathbf{H}}^{cal}(\mathbf{T}) = \sum_{g,g'=1}^{G} f_m(\mathbf{H}\mathbf{M}_g \mathbf{D}\mathbf{R}_m \mathbf{O}_m) \overline{f_m(\mathbf{H}\mathbf{M}_{g'} \mathbf{D}\mathbf{R}_m \mathbf{O}_m)} e^{2\pi i \mathbf{H} \left((\mathbf{M}_g - \mathbf{M}_{g'})^{\mathbf{T} + \mathbf{t}_g - \mathbf{t}_{g'}} \right)}$$

$$= \sum_{g,g'=1}^{G} u_g^m(\mathbf{H}) \overline{u_{g'}^m(\mathbf{H})} e^{2\pi i \mathbf{H} \left(\mathbf{M}_g - \mathbf{M}_{g'} \right)^{\mathbf{T}}}.$$

Several translation functions may be calculated ("centered" variables are denoted by $\overline{\overline{I_{\mathbf{H}}}} = I_{\mathbf{H}} - \langle I_{\mathbf{H}} \rangle$):

• centered-overlap

$$CO(\mathbf{T}) = \sum_{\mathbf{H}} \overline{\overline{I_{\mathbf{H}}^{obs}}} \times \overline{\overline{I_{\mathbf{H}}^{cal}(\mathbf{T})}}$$

$$\propto \sum_{g,g'=1}^{G} \sum_{\mathbf{H}} \overline{\overline{I_{\mathbf{H}}^{obs}}} \overline{u_g^m(\mathbf{H})} u_{g'}^m(\mathbf{H}) e^{-2\pi i \mathbf{H} \left(\mathbf{M}_g - \mathbf{M}_{g'}\right) \mathbf{T}}$$

• Harada-Lifchitz

$$HL(\mathbf{T}) = \left(\sum_{\mathbf{H}} \overline{\overline{I_{\mathbf{H}}^{obs}}} imes \overline{\overline{I_{\mathbf{H}}^{cal}(\mathbf{T})}} \right) \bigg/ \sum_{\mathbf{H}} I_{\mathbf{H}}^{cal}(\mathbf{T})$$

• correlation-coefficient

$$CC(\mathbf{T}) = \left(\sum_{\mathbf{H}} \overline{\overline{I_{\mathbf{H}}^{obs}}} \times \overline{\overline{I_{\mathbf{H}}^{cal}(\mathbf{T})}}\right) / \sqrt{\left(\sum_{\mathbf{H}} \overline{\overline{I_{\mathbf{H}}^{obs}}}^{2}\right) \times \left(\sum_{\mathbf{H}} \overline{\overline{I_{\mathbf{H}}^{cal}(\mathbf{T})}}^{2}\right)}$$

• phased-translation

1. without "external" phases

$$PT(\mathbf{T}) = \sum_{g,g'=1}^{G} \sum_{\mathbf{H}} \left(|F_{\mathbf{H}}^{obs}/u_g^m(\mathbf{H})| + |F_{\mathbf{H}}^{obs}/u_{g'}^m(\mathbf{H})| - 2 SCAL \right) \times \overline{u_g^m(\mathbf{H})} u_{g'}^m(\mathbf{H}) e^{-2\pi i \mathbf{H}(\mathbf{M}_g - \mathbf{M}_{g'})\mathbf{T}}$$

2. with "external" phases

$$PTF(\mathbf{T}) = \sum_{\mathbf{H}} |F^{obs}_{\mathbf{H}}| \; e^{i\phi^{ext}_{\mathbf{H}}} \times \overline{F^{cal}_{\mathbf{H}}(\mathbf{T})}$$

- many-body translation
 - 1. phased-translation

$$PTN(\mathbf{T}) = \sum_{\mathbf{H}} \left(\left| \frac{F_{\mathbf{H}}^{obs}}{F_{\mathbf{H}}^{fix}} \right| - SCAL \right) F_{\mathbf{H}}^{fix} \times \overline{F_{\mathbf{H}}^{cal}(\mathbf{T})}$$

2. for all others, replace

$$F_{\mathbf{H}}^{cal}(\mathbf{T}) \to F_{\mathbf{H}}^{cal}(\mathbf{T}) + F_{\mathbf{H}}^{fix}$$

Calling command: ./e/traing {INP} {OUT}

Input: $./i/{INP}.i1$ = input described below.

./f/xudi = binary file of packed and sorted H,K,L,F^{obs}.

 $./f/tabl\{\#\}$ = binary files of molecular scattering factors; $\{\#\} = 1,NTYP.$

Output: $./o/{OUT}.s = translation function output.$

To recover the last fast translation function map, erase in script ./e/traing , the symbol "#" in line "#mv \$AMOREF/fort.94 tramap". ./tramap is a binary file with several registers:

```
\begin{array}{l} {\rm real\ tramap(nx,ny,nz)} \\ {\rm write(file)\ nx,ny,nz,a,b,c,alpha,beta,gamma} \\ {\rm do\ iz}{=}1{\rm ,nz} \\ {\rm write(file)\ ((tramap(ix,iy,iz),ix}{=}1{\rm ,nx}){\rm ,iy}{=}1{\rm ,ny})} \\ {\rm enddo} \end{array}
```

where:

```
\begin{array}{lll} nx,ny,nz & = & number\ of\ sampling\ points\ in\ each\ direction. \\ a,b,c,alpha,beta,gamma & = & cell\ parameters\ (in\ \mathring{A}\ \ and\ degrees). \end{array}
```

Input: file ./i/{INP}.i1

```
traing +*+*+*+*+*+*+*
7 1 1 0 1 0 1 1 :printing
10 9 :logical units
* D44HEL **
99.700 167.300 84.700 90.000 90.000 90.000
x,y,z * 1/2+x,1/2-y,-z * 1/2-x,-y,1/2+z * -x,1/2+y,1/2-z * end
0
95.0 0.0
15.00 3.50 0.88 1.00
c-o 0.0
0.50 \quad 30 \quad 1.e-4
 > 1 102.3 25.7
                12.8 \quad 0.0755 \quad 0.3081
                                     0.4560 27.6 52.1 54.0 42.0
> 1 135.5 43.0 320.5 0.4613 0.2053
                                     0.0096
                                            38.6 48.1
                                                      41.1 \quad 37.0
# 2 73.6 68.9 346.3 0.0000 0.0000
                                     0.0000
                                             7.6
c-o 0.0
0.50 30 1.e-4
 > 1 102.3 25.7
                12.8 \quad 0.0755 \quad 0.3081
                                    0.4560 27.6 52.1 54.0 42.0
 > 1 135.5 43.0 320.5 0.4613 0.2053
                                     0.0096
                                            38.6 48.1
                                                      41.1 \quad 37.0
# 2
      74.8 61.6 309.9 0.0000 0.0000
                                    0.0000
                                             4.0
. . .
```

- 1) Keyword (format A7) = 'traing'.
- 2) Printing options.
- 3) LUN1 LUN2

Logical units (see script ./e/traing):

LUN1 = input binary file of packed and sorted H,K,L,F^{obs} (./f/xudi). LUN2 = translation function output (./o/{OUT}.s).

- 4) Title (format A80).
- 5) Cell.
- 6) Symmetry operations (lower case), finishing '* end'.
- 7) NORT

Code to define an orthogonal reference frame.

8) PERC BADD

PERC = uses only the PERC % highest F^{obs}.

BADD = B-factor added to F^{obs} (e.g. -5 to sharpen data).

9) DMAX DMIN TMIN SHAR

DMAX,DMIN = data resolution limits.

TMIN = fast translation function resolution (default value is

DMIN/4).

SHAR = Shannon rate (the greater SHAR, the finer the mesh).

Defines the crystal cell sampling as $NX \approx 2 \times a / (TMIN/SHAR)$

 $NY \approx 2 \times b / (TMIN/SHAR)$

 $NZ \approx 2 \times c / (TMIN/SHAR)$

Then add this information which is extracted from ROTING, TRAING or FITING outputs:

10) NBOD

Number of molecules (n-body mode).

11) TKEY SCAL (format A5,*)

'c-o' computes centered-overlap;

TKEY = computes phased-translation ('p-t-f' when phases are available);

'h-l' computes Harada-Lifchitz translation function;

'c-c' computes correlation-coefficient.

- SCAL = for phased-translation, to scale the phasing-model subtraction.
- 12) CUTT NPIC DELT

CUTT = cutoff in fast translation function output; first selects all peaks above CUTT × maximum-peak-height of 'c-o', 'p-t',

'h-l' or 'c-c' fast translation function.

NPIC = maximum number of peaks to output of translation function.

The program computes correlations and R-factors.

DELT = used in peak-search to avoid spurious peaks.

13) # $\mu_m \phi_m \theta_m \psi_m x_m y_m z_m$ (NBOD cards; m = 1, NBOD)

This is a formatted line. The format is decided by the user when installing the package. If NBOD = 1 search is done over the Cheshire cell.

Otherwise last will be translated over whole cell while keeping the others fixed.

 μ_m = model identification number; also logical-unit identifier

for molecular scattering factors corresponding to the *m*-th molecule.

Usually, logical-unit = $\mu_m + 10$.

 $\phi_m \theta_m \psi_m = \text{Euler angles for } m\text{-th molecule.}$

 $x_m y_m z_m$ = translations (fractionnary) for m-th molecule. For the last

one, read but not used.

Repeat 10) — 13) for other positions and orientations.

FITING

FITING performs rigid-body refinement. Minimizes

$$\sum_{\mathbf{H}} \left(F_{\mathbf{H}}^{obs} - \frac{e^{+B|\mathbf{H}|^2}}{Scale} | \sum_{m} F_{\mathbf{H}}^{cal(m)}(\phi_m, \theta_m, \psi_m, x_m, y_m, z_m) | \right)^2$$

with respect to B, Scale and rotation and translation parameters.

Calling command: ./e/fiting {INP} {OUT}

 $\label{eq:input:input:input} \mbox{Input:} \quad ./i/\{\mbox{INP}\}.i1 = \mbox{input described below}.$

 $./f/xudi = binary file of packed and sorted H,K,L,F^{obs}.$

./f/tabl{#} = binary files of molecular scattering factors; {#} = 1,NTYP.

Output: $./o/{OUT}.s = fast rigid-body refinement output.$

Input: file ./i/{INP}.i1

```
fiting +*+*+*+*+*+*+*
7 1 1 0 1 0 1 1 :printing
10 9 :logical units
* D44HEL **
99.700 167.300 84.700 90.000 90.000 90.000
x,y,z * 1/2+x,1/2-y,-z * 1/2-x,-y,1/2+z * -x,1/2+y,1/2-z * end
0
95.0 \quad 0.0
15.00 \quad 3.50
inertia tensors 2
 * 1 140.3 100.2 78.1
 * 2
             66.1 \quad 50.0
      80.0
0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 1 \quad 1
1 20 0.04
 # 1 102.3 25.7
                  12.8 \quad 0.0755 \quad 0.3081
                                        0.4560 27.6 52.1 54.0
                                                                 42.0
 # 1 135.5 43.0 320.5 0.4613 0.2053
                                        0.0096
                                                38.6 48.1
                                                           41.1
                                                                 37.0
# 2
       74.8 61.6 309.9 0.2951 0.9939 0.8339
                                                43.9 45.5 41.8
                                                                 28.0
. . .
```

- 1) Keyword (format A7) = 'fiting '.
- 2) Printing options.
- 3) LUN1 LUN2

Logical units (see script ./e/fiting):

LUN1 = input binary file of packed and sorted H,K,L,F^{obs} (./f/xudi).

 $LUN2 = fast rigid-body refinement output (./o/{OUT}.s).$

- 4) Title (format A80).
- 5) Cell.
- 6) Symmetry operations (lower case), finishing '* end'.
- 7) NORT Code to define an orthogonal reference frame.
- 8) PERC BADD

PERC = uses only the PERC % highest F^{obs}.

BADD = B-factor added to F^{obs} (e.g. -5 to sharpen data).

9) DMAX DMIN

DMAX,DMIN = resolution limits.

10) NTYP (format *, after column 15)

Number of different models whose positions are to be refined.

11) * $m Q_{xx}^m Q_{yy}^m Q_{zz}^m Q_{xy}^m Q_{xz}^m Q_{yz}^m$ (NTYP cards; m=1,NTYP) This is a formatted line. The format is decided by the user when installing the package.

m = model identification number.

 Q_{ii}^m = principal moments of inertia for m-th model.

Then add this information which is extracted from TRAING or FITING outputs (or ROTING for space group P1):

12) NBOD

Number of molecules (n-body mode).

13) Refinement flags (7 flags).

Flags for refinement of B-factor, Euler angles and translations.

- $= \begin{vmatrix} 0 & (\text{no refinement}); \\ 1 & (\text{refinement}). \end{vmatrix}$
- 14) NCYC NITE RMSS

NCYC = number of times the NBOD bodies are alternately refined.

NITE = number of iterations in the least-squares procedure.

RMSS = root-mean-square shift (in Å). Least-squares stops if the rms. correction to positions is less than RMSS.

15) # $\mu_m \phi_m \theta_m \psi_m x_m y_m z_m$ (NBOD cards; m = 1, NBOD)

This is a formatted line. The format is decided by the user when installing the package. If NBOD > 1, last is refined first, while the others are kept fixed; then proceeds cyclically.

 μ_m = model identification number; also logical-unit identifier for molecular scattering factors corresponding to the m-th molecule.

Usually, logical-unit = $\mu_m + 10$.

 $\phi_m \theta_m \psi_m$ = Euler angles for m-th molecule.

 $x_m y_m z_m$ = translations (fractionnary) for m-th molecule.

Repeat 12) to 15) for other positions.

MR2IC

MR2IC reads the rotation and translation applied by TABLING to the input models, and the refined rotations and translations output from FITING, to work out the final rotations and translations parameters to apply to the initial models.

Calling command: ./e/mr2ic {INP} {OUT}

Standard input: ./e/mr2ic

Input: ./d/data.d = ascii file of main $\mathcal{AMoR}_{\varepsilon}$ input.

./o/tabl{#}.s = ascii file of TABLING outputs; $\{\#\} = 1,NTYP.$

 $./o/{INP}.s$ = ascii file of FITING output.

Output: $./o/{OUT}.s = output positional parameters.$

Standard Input: (file ./e/mr2ic)

mr2ic 1

Description

1) OKEY NUMF (format A6,*)

OKEY = 'mr2ic'

NUMF = selects up to a maximum of NUMF positions to output

(in decreasing order of correlation).

OIC

OIC creates inputs to the main molecular replacement programs by selecting and combining potential solutions, which are sorted according to the values of the correlation coefficient.

Calling command:

```
      ./e/oic
      {NOM}
      {#}
      {OUT}
      ; 3 arguments.

      ./e/oic
      {NOM}
      {IN1}
      {OUT}
      ; 3 arguments.

      ./e/oic
      {NOM}
      {IN1}
      {IN2}
      {OUT}
      ; 4 arguments.
```

Five situations are possible according to **{NOM}** and number of arguments:

- for ROTING inputs, model dimensions are read from file ./o/tabl{#}.s; 3 arguments.
- for one-body TRAING inputs, orientations to translate are read from file ./o/{IN1}.s; 3 arguments.
- for n-body TRAING inputs, orientations are read from file ./o/{IN1}.s, and the fixed position from file ./o/{IN2}.s. If orientations are read from a n-body output, only those corresponding to the last body are taken into account; 4 arguments.
- for n-body TRAING inputs, where the orientations and the fixed position are read from the same file ./o/{IN1}.s; 3 arguments.
- for FITING inputs, positions to refine are read from file ./o/ $\{IN1\}$.s; 3 arguments.

The OIC program needs the ./o/tabl{#}.s file to define the integration radius and the model cell for cross-rotation function calculations. This file is not created if the molecular scattering factors of the search model electron density is not calculated with TABLING.

Three different input modes:

Input: file ./i/ ${NOM}$.i2 (ROTING mode)

```
oic roting +*+*+*+*+*+*+*
* D44HEL **
model: 1
15.00   3.50
1.0
2   10
2.5
0.5   1000
```

- 1) Keyword defining mode (format A10) = 'oic roting'.
- 2) Title (format A80).
- 3) MTYP (format *, after column 7) Model-identification number.
- 4) DMAX DMIN

Resolution limits (in Å).

5) RATE

Defines the integration radius as RATE \times Molrad, where Molrad is the radius of the smallest sphere, with origin at CoM, containing the whole molecule.

6) LMINs LMINf

several rotation functions are calculated, where the spherical-harmonics expansions begin with LMINs $\leq \ell \leq$ LMINf; the ℓ -expansion controls the angular resolution.

7) STEP

Step size for ϕ , θ and ψ (in degrees).

- 8) CUTR NPIC
 - CUTR = cutoff in rotation function output; first selects all peaks above CUTR × maximum-peak-height.
 - NPIC = maximum number of peaks to output of rotation function.

Input: file ./i/{NOM}.i2 (TRAING mode)

```
oic traing +*+*+*+*+*+*+*
* D44HEL **
n-body-s 1
p-t 1.0
0.0 10
15.00 3.50
0.5 30
fuzz: 2.0
over: 20.0
```

- Keyword defining mode (format A10) = 'oic traing'.
- 2) Title (format A80).
- BKEY RANK (format A10,*)

'one-body' BKEY = keyword defining mode. Three possibilities: 'n-body 'n-body-s

> The last one is for the particular case of n-body translations where the orientations to translate and the fixed position are read from the same file. When the number of arguments is 4, the OIC procedure uses "sed" to erase '-s'.

RANK = takes as fixed position the one that appears in RANK-th order of decreasing correlation (for n-body).

TKEY SCAL (format A5,*)

TKEY =

| 'p-t' computes centered-overlap; |
| 'p-t' computes phased-translation ('p-t-f' when phases are available); |
| 'h-l' computer II

'c-c' computes correlation-coefficient.

= for phased-translation, to scale the phasing-model subtraction.

CORR NUMR

CORR =cutoff to select only those solutions with correlation coefficient greater than CORR.

selects up to a maximum of NUMR orientations for input NUMR =to translation (in decreasing order of correlation).

DMAX DMIN

Resolution limits (in Å).

CUTT NPIC

CUTT = cutoff in fast translation function output; first selects all

peaks above CUTT × maximum-peak-height of 'c-o', 'p-t',

'h-l' or 'c-c' fast translation function.

NPIC number of peaks to output of translation function. The program computes correlations and R-factors.

8) CUTO (format *, after column 5)

Cutoff to eliminate orientations to translate differing by less than CUTO degrees.

9) CUTD (format *, after column 5) Cutoff to eliminate fixed positions with CoM-CoM distance less than CUTD Å (for n-body).

Input: file ./i/{NOM}.i2 (FITING mode)

- 1) Keyword defining mode (format A10) = 'oic fiting'.
- 2) Title (format A80).
- 3) CORR NUMT

CORR = cutoff to select only those solutions with correlation

coefficient greater than CORR.

NUMT = selects up to a maximum of NUMT positions to refine (in decreasing order of correlation).

4) DMAX DMIN

Resolution limits (in Å).

5) NCYC NITE RMSR

NCYC = number of times the n-bodies are alternately refined.

NITE = number of iterations in the least-squares procedure.

RMSR = least-squares stops if the rms. correction to positions is less than $RMSR \times DMIN$.

6) CUTO (format *, after column 5)

Cutoff to eliminate orientations differing by less than CUTO degrees (for space group P1).

7) CUTD (format *, after column 5)

Cutoff to eliminate positions with CoM-CoM distance less than CUTD $\hbox{Å}.$

The OIC_ROTING, OIC_TRAING and OIC_FITING procedures

oic_roting, oic_traing and oic_fiting are the concatenations of OIC with the main molecular replacement programs.

OIC_ROTING

oic_roting computes cross-rotation function.

Calling command: ./e/oic_roting {NOM} {#} {OUT}

Description

```
./i/{NOM}.i2 = input to OIC, ROTING mode.
{#} = model number.
./i/rot.i1 = input to ROTING program.
./o/{OUT}.s = cross-rotation function output.
```

OIC_TRAING

oic_traing computes fast translation functions.

Calling command: ./e/oic_traing {NOM} {ANG} {OUT}

Description

Calling command: ./e/oic_traing {NOM} {ANG} {POS} {OUT}

```
equivalent to | ./e/oic {NOM} {ANG} {POS} tra | ./e/traing tra {OUT}
```

 $./i/{NOM}.i2 = input to OIC, TRAING mode.$

./o/{ANG}.s = filename of ROTING, TRAING or FITING output; orientations to translate (and fixed positions in n-body cases) are read from this file. If the orientations are read from a n-body output, only those corresponding

to the last body are taken into account.

./o/ $\{POS\}$.s = $(\{POS\} \neq \{ANG\})$ filename of TRAING or FITING output (or ROTING for space group P1); fixed positions are read from this file.

./i/tra.i1 = input to TRAING program.

./o/{OUT}.s = translation function output.

OIC_FITING

oic_fiting performs fast rigid-body refinements.

Calling command: ./e/oic_fiting {NOM} {POS} {OUT}

 $./i/{NOM}.i2 = input to OIC, FITING mode.$

./o/{POS}.s = filename of TRAING or FITING output (or ROTING for space group P1); positions to be refined are read

from this file.

./i/fit.i1 = input to FITING program.

./o/{OUT}.s = fast rigid-body refinement output.